

12.10

3-10: Find the Maclaurin series for $f(x)$ using the definition of a Maclaurin series. [Assume that f has a power series expansion. Do not show that $R_n(x) \rightarrow 0$.] Also find the associated radius of convergence.

3. $f(x) = \cos x$

4. $f(x) = \sin 2x$

5. $f(x) = 1 + x^{-3}$

6. $f(x) = \ln 1 + x$

7. $f(x) = e^{5x}$

8. $f(x) = xe^x$

11-18: Find the Taylor series for $f(x)$ centered at the given value of a . [Assume that f has a power series expansion. Do not show that $R_n(x) \rightarrow 0$.]

11. $f(x) = 1 + x + x^2, a = 2$

12. $f(x) = x^3, a = -1$

13. $f(x) = e^x, a = 3$

14. $f(x) = \ln x, a = 2$

15. $f(x) = \cos x, a = \pi$

16. $f(x) = \sin x, a = \frac{\pi}{2}$

17. $f(x) = \sqrt[3]{x}, a = 9$

18. $f(x) = x^{-2}, a = 1$

23-28: use a Maclaurin series derived in this section to obtain the Maclaurin series for the given function.

23. $f(x) = \cos \pi x$

24. $f(x) = e^{-x/2}$

25. $f(x) = x \tan^{-1} x$

26. $f(x) = \sin x^4$

27. $f(x) = x^2 e^{-x}$

28. $f(x) = x \cos 2x$