

NAME THE NASTIEST THEOREM IN MATHEMATICS.

For each function $f(x)$ on the given closed interval $[a, b]$,

a) find the value of the slope $m = \frac{f(b) - f(a)}{b - a}$,

b) find the value(s) of $c \in (a, b)$, if any, such that $f'(c) = \frac{f(b) - f(a)}{b - a}$,

c) match with a graph that illustrates the function, secant and tangent lines.

Example: $f(x) = 2x - x^2$; $[0, 3]$

$f(0) = 0$ and $f(3) = -3$

find the slope $m = \frac{f(b) - f(a)}{b - a}$

$m = \frac{f(3) - f(0)}{3 - 0} = \frac{-3 - 0}{3 - 0} = -1, \therefore f'(c) = -1$

$f(x) = 2x - x^2$

$f'(x) = 2 - 2x$

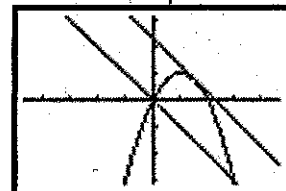
since $f'(c) = -1$

$2 - 2c = -1$

$-2c = -3$

$c = 1.5$

Graph:

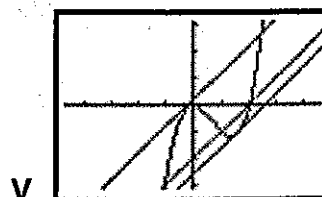
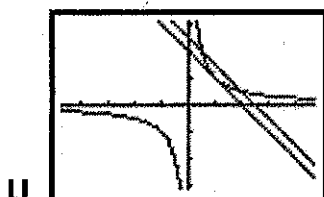
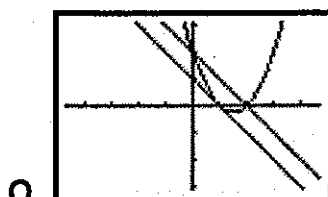
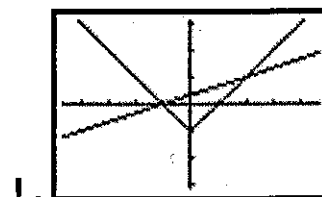
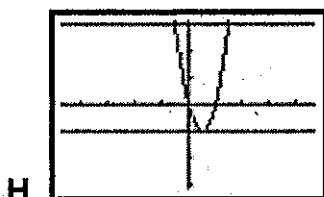
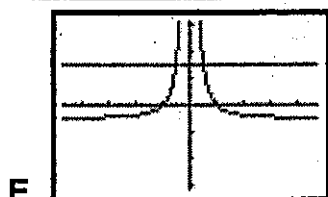


Functions.

| | |
|--------------------------------------|--|
| 1) $f(x) = x^2 - 3x + 2$; $[0, 2]$ | 2) $f(x) = 4x^2 - 4x$; $[-0.5, 1.5]$ |
| 3) $f(x) = \frac{1}{x}$; $[0.5, 2]$ | 4) $f(x) = (1 - x^2)/2x^2$; $[-0.5, 0.5]$ |
| 5) $f(x) = x - 1$; $[-1, 2]$ | 6) $f(x) = x^3 - 2x^2$; $[-1, 2]$ |

Values a) of the slope, b) of c , and c) the graphs.

| | | | | | |
|-------|-------|------------------|------------|-------------------------------|------------------|
| A. -1 | B. -2 | C. -3 | E. 1 | F. 3 | H. $\frac{1}{3}$ |
| J. 5 | M. 0 | N. $\frac{1}{2}$ | O. ± 1 | R. $\frac{2 \pm \sqrt{7}}{3}$ | T. no value |



7) The value of c as described above will exist if the function $f(x)$ is

| | | |
|-----------------------------|---------------------------------|--|
| A. continuous on $[a, b]$. | C. differentiable on (a, b) . | E. Both continuous on $[a, b]$, and differentiable on (a, b) . |
|-----------------------------|---------------------------------|--|

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|----|----|----|
| | | |
| 5b | 5a | 1b |

| | | |
|----|---|-------|
| | | |
| 2a | 7 | 1a 2b |

| | | |
|----|----|----------|
| | | |
| 6c | 3a | 5c 3c 4c |

| | | |
|----|----|----------------|
| | | |
| 4b | 2c | 3b 1c 6b 6a 4a |