Section 4.7

Integration using Completing the square

Let's review how to complete the square

•
$$(x + 5)^2 =$$

$$x^2 - 12x + 36 =$$

•
$$x^2 + 4x + 7$$

$$3x^2 - 30x + 45$$

•
$$x^2 - 8x + 9$$

$$x^2 + 5x - 3$$

•
$$x^2 + 12x - 4$$

$$2x^2 + 15x + 1$$

$$\int \frac{1}{x^2 - 6x + 13} dx$$

• Should I do long division?

No, not an improper fraction.

• U-sub?

No, numerator is not the derivative of denominator

Partial Fractions?

No, can't factor the denominator.

• What if I complete the square of the denominator?

$$\int \frac{1}{x^2 - 6x + 13} dx$$

$$\int \frac{2x+2}{x^2+8x+20} dx$$

Should I do long division?

No, not an improper fraction.

Partial Fractions?

No, can't factor the denominator.

• U-sub?

No, numerator is not the derivative of denominator,

• But could I make it the derivative?

$$\int \frac{2x+2}{x^2+8x+20} dx$$

Find the area of the region bounded by the graph of $f(x) = \frac{1}{\sqrt{1-2x-x^2}}$ and the lines x = -1 and x = 0.