

Day 5 Homework

Use your calculator on problems 7–11 only.

1. If $x = e^{2t}$ and $y = \sin(3t)$, find $\frac{dy}{dx}$ in terms of t .
2. Write an integral expression to represent the length of the path described by the parametric equations $x = \cos^3 t$ and $y = \sin^2 t$ for $0 \leq t \leq \frac{\pi}{2}$.
3. For what value(s) of t does the curve given by the parametric equations $x = t^3 - t^2 - 1$ and $y = t^4 + 2t^2 - 8t$ have a vertical tangent?
4. For any time $t \geq 0$, if the position of a particle in the xy -plane is given by $x = t^2 + 1$ and $y = \ln(2t + 3)$, find the acceleration vector.
5. Find the equation of the tangent line to the curve given by the parametric equations $x(t) = 3t^2 - 4t + 2$ and $y(t) = t^3 - 4t$ at the point on the curve where $t = 1$.
6. If $x(t) = e^t + 1$ and $y = 2e^{2t}$ are the equations of the path of a particle moving in the xy -plane, write an equation for the path of the particle in terms of x and y .
7. A particle moves in the xy -plane so that its position at any time t is given by $x = \cos(5t)$ and $y = t^3$. What is the speed of the particle when $t = 2$?
8. The position of a particle at time $t \geq 0$ is given by the parametric equations $x(t) = \frac{(t-2)^3}{3} + 4$ and $y(t) = t^2 - 4t + 4$.
 - (a) Find the magnitude of the velocity vector at $t = 1$.
 - (b) Find the total distance traveled by the particle from $t = 0$ to $t = 1$.
 - (c) When is the particle at rest? What is its position at that time?
9. An object moving along a curve in the xy -plane has position $(x(t), y(t))$ at time $t \geq 0$ with $\frac{dx}{dt} = 1 + \tan(t^2)$ and $\frac{dy}{dt} = 3e^{\sqrt{t}}$. Find the acceleration vector and the speed of the object when $t = 5$.
10. A particle moves in the xy -plane so that the position of the particle is given by $x(t) = t + \cos t$ and $y(t) = 3t + 2\sin t$, $0 \leq t \leq \pi$. Find the velocity vector when the particle's vertical position is $y = 5$.
11. An object moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with $\frac{dx}{dt} = 2\sin(t^3)$ and $\frac{dy}{dt} = \cos(t^2)$ for $0 \leq t \leq 4$. At time $t = 1$, the object is at the position $(3, 4)$.
 - (a) Write an equation for the line tangent to the curve at $(3, 4)$.
 - (b) Find the speed of the object at time $t = 2$.
 - (c) Find the total distance traveled by the object over the time interval $0 \leq t \leq 1$.
 - (d) Find the position of the object at time $t = 2$.