

Day 6 Homework

Use your calculator only on problems 3–7.

- The position of a particle at any time $t \geq 0$ is given by $x(t) = t^2 - 2$, $y(t) = \frac{2}{3}t^3$.
 - Find the magnitude of the velocity vector at $t = 2$.
 - Set up an integral expression to find the total distance traveled by the particle from $t = 0$ to $t = 4$.
 - Find $\frac{dy}{dx}$ as a function of x .
 - At what time t is the particle on the y -axis? Find the acceleration vector at this time.
- An object moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with the velocity vector $v(t) = \left(\frac{1}{t+1}, 2t\right)$. At time $t = 1$, the object is at $(\ln 2, 4)$.
 - Find the position vector.
 - Write an equation for the line tangent to the curve when $t = 1$.
 - Find the magnitude of the velocity vector when $t = 1$.
 - At what time $t > 0$ does the line tangent to the curve at $(x(t), y(t))$ have a slope of 12?
- A particle moving along a curve in the xy -plane has position $(x(t), y(t))$, with $x(t) = 2t + 3\sin t$ and $y(t) = t^2 + 2\cos t$, where $0 \leq t \leq 10$. Find the velocity vector at the time when the particle's vertical position is $y = 7$.
- A particle moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with $\frac{dx}{dt} = 1 + \sin(t^3)$. The derivative $\frac{dy}{dt}$ is not explicitly given. For any time t , $t \geq 0$, the line tangent to the curve at $(x(t), y(t))$ has a slope of $t + 3$. Find the acceleration vector of the object at time $t = 2$.

5. An object moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with $\frac{dx}{dt} = \cos(e^t)$ and $\frac{dy}{dt} = \sin(e^t)$ for $0 \leq t \leq 2$. At time $t = 1$, the object is at the point $(3, 2)$.
- Find the equation of the tangent line to the curve at the point where $t = 1$.
 - Find the speed of the object at $t = 1$.
 - Find the total distance traveled by the object over the time interval $0 \leq t \leq 2$.
 - Find the position of the object at time $t = 2$.
6. A particle moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with $\frac{dx}{dt} = \sin(t^3 - t)$ and $\frac{dy}{dt} = \cos(t^3 - t)$. At time $t = 3$, the particle is at the point $(1, 4)$.
- Find the acceleration vector for the particle at $t = 3$.
 - Find the equation of the tangent line to the curve at the point where $t = 3$.
 - Find the magnitude of the velocity vector at $t = 3$.
 - Find the position of the particle at time $t = 2$.
7. An object moving along a curve in the xy -plane has position $(x(t), y(t))$ at time t with $\frac{dy}{dt} = 2 + \sin(e^t)$. The derivative $\frac{dx}{dt}$ is not explicitly given. At $t = 3$, the object is at the point $(4, 5)$.
- Find the y -coordinate of the position at time $t = 1$.
 - At time $t = 3$, the value of $\frac{dy}{dx}$ is -1.8 . Find the value of $\frac{dx}{dt}$ when $t = 3$.
 - Find the speed of the object at time $t = 3$.