

# WHY DID THE $e^x$ FUNCTIONS FAIL TO INTEGRATE INTO A COMMUNITY OF $\ln(x)$ FUNCTIONS?

Match each indefinite integral with an anti-derivative.

1) $\int e^x dx$ D	2) $2 \int e^x dx$ E	3) $\frac{1}{2} \int e^x dx$ A	4) $\int e^{2x} dx$ C	5) $3 \int e^{3x} dx$ G
6) $\int 2^x dx$ T	7) $\int 3^x dx$ Y	8) $3 \int 2^x dx$ U	9) $\int 2^{3x} dx$ W	10) $\int 2^x \ln 2 dx = \ln 2 \int 2^x dx = \frac{\ln 2 \cdot 2^x}{\ln 2}$
11) $\int e^{2x+1} dx$ L	12) $\int e^{3x+1} dx$ H	13) $\int \frac{e^x+1}{e^x} dx$ N	14) $\int (e^x - 1)(e^{-x} + 1) dx$ O	

Anti-derivatives.

A. $\frac{1}{2}e^x + C$	C. $\frac{1}{2}e^{2x} + C$	D. $e^x + C$	E. $2e^x + C$	G. $e^{3x} + C$
E. $2^x + C$	L. $\frac{1}{2}e^{2x+1} + C$	H. $\frac{1}{3}e^{3x+1} + C$	N. $x - e^{-x} + C$	O. $e^x + e^{-x} + C$
S. $e^x - e^{-x} + C$	T. $\frac{2^x}{\ln 2} + C$	U. $\frac{3 \cdot 2^x}{\ln 2} + C$	W. $\frac{2^{3x}}{3 \ln 2} + C$	Y. $\frac{3^x}{\ln 3} + C$

T H E Y      W O U L D N ' T      C H A N G E  
 6 12 10 7      9 14 8 11 1 13      6      4 12 3 13 5 2

# WHY IS $\int \frac{d(\text{CABIN})}{\text{CABIN}}$ LIKE A HOUSEBOAT?

Match each indefinite integral with an anti-derivative.

1) $\int \frac{dx}{x}$ C	2) $\int \frac{2dx}{x}$ B	3) $\int \frac{dx}{2x}$ A	4) $\int \frac{dx}{x^2}$ F	5) $\int \frac{dx}{x^3}$ E
6) $\int \frac{dx}{x-1}$ I	7) $\int \frac{dx}{1-x}$ L	8) $\int \frac{2dx}{3x-1}$ P	9) $\int \frac{3dx}{2x-1}$ S	
10) $\int \frac{x+1}{x} dx$ O	11) $\int \frac{x^2-1}{x} dx$ N	12) $\int \frac{x+1}{x^2} dx$ U	13) $\int (x-1)(x^{-1}+1) dx$ N	

Anti-Derivatives.

A. $\frac{1}{2} \ln x  + C$	B. $2 \ln x  + C$	C. $\ln x  + C$	E. $-\frac{1}{2}x^{-2} + C$	G. $-x^{-1} + C$
I. $\ln x-1  + C$	L. $-\ln 1-x  + C$	N. $\frac{1}{2}x^2 - \ln x  + C$	O. $x + \ln x  + C$	
P. $\frac{2}{3} \ln 3x-1  + C$	S. $\frac{3}{2} \ln 2x-1  + C$	T. $\ln 1-x  + C$	U. $\ln x  - \frac{1}{x} + C$	

L N ( C A B I N ) + C  
 7 13      1 3 2 6 13      1

L O G      C A B I N      P L U S      S E A  
 7 10 4      1 3 2 6 11      8 7 12 9      9 5 3

Top

(5)

4) let  $u = 2x$   $\frac{1}{2} \int e^u du = \frac{1}{2} e^{2x} + C$   
 $\frac{du}{dx} = 2$   
 $\frac{du}{2} = dx$

5) let  $u = 3x$   $3 \cdot \frac{1}{3} \int e^u du = e^{3x} + C$   
 $\frac{du}{dx} = 3$   
 $\frac{du}{3} = dx$

9) let  $u = 3x$   $\frac{1}{3} \int 2^u du = \frac{1}{3} \cdot \frac{2^u}{\ln 2} + C$   
 $\frac{du}{dx} = 3$   
 $\frac{du}{3} = dx$

11) let  $u = 2x+1$   $\frac{1}{2} \int e^u du = \frac{1}{2} e^{2x+1} + C$   
 $\frac{du}{dx} = 2$   
 $\frac{du}{2} = dx$

12) let  $u = 3x+1$   $\frac{1}{3} \int e^u du = \frac{1}{3} e^{3x+1} + C$   
 $\frac{du}{dx} = 3$   
 $\frac{du}{3} = dx$

13)  ~~$u = e^x + 1$   $\int \frac{e^{x+1}}{e^x} dx = \int (1 + e^{-x}) dx$~~  let  $u = -x$   
 $\frac{du}{dx} = e^x$   $\int dx + \int e^{-x} dx$   $\frac{du}{dx} = -1$   
 $\frac{du}{e^x} = dx$   $\int e^{-x}(e^x + 1) dx$   $-du = dx$   
 $\int dx + \int e^{-x} dx$   
 $x + \int e^u du$   
 $x - e^u + C = x - e^{-x} + C$

14)  $\int (e^0 - e^{-x} + e^x - 1) dx$   
 $\int (e^0 - e^{-x} + e^x - 1) dx = \int e^0 dx - \int e^{-x} dx + \int e^x dx - \int 1 dx$   
 $e^0 = 1$   
 $\frac{du}{dx} = -1$   
 $-du = dx$

Bottom  
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$$6) u = x-1 \quad \int \frac{1}{u} du \\ \frac{du}{dx} = 1 \quad \ln|x-1| + C \\ du = dx$$

$$8) u = 3x+1 \quad \frac{2}{3} \ln|3x+1| + C \\ \frac{du}{dx} = 3 \\ \frac{1}{3} du = dx$$

$$9) u = 2x-1 \quad \frac{3}{2} \ln|2x-1| + C \quad 10) \int \left(1 + \frac{1}{x}\right) dx \\ \frac{1}{2} du = dx$$

$$x + \ln|x| + C$$

$$11) \int \left(x - \frac{1}{x}\right) dx$$

$$\frac{1}{2} x^2 - \ln|x| + C$$

$$12) \int \left(\frac{1}{x} + \frac{1}{x^2}\right) dx$$

$$\ln|x| - x^{-1} + C$$

$$13) \int \left(x^0 - \frac{1}{x} + x - 1\right) dx \\ -\ln|x| + \frac{1}{2} x^2 + C$$

# IF $U = \frac{1}{2}(\text{LOOP})^2$ , THEN $DU = (?)$ .

Choose a function to substitute for u.

1) $\int 2x(x^2 + 1)^5 dx$	2) $\int \frac{2x}{x^2 + 1} dx$	3) $\int 2x\sqrt{x^2 + 1} dx$	4) $\int 3x^2(x^3 + 1)^5 dx$
5) $\int \sin^3(x)\cos(x) dx$	6) $\int \frac{\cos(x)}{\sin(x)} dx$	7) $-\int \sin(x)e^{\cos(x)} dx$	8) $-\int \frac{\sin(x)}{\cos^2(x)} dx$
9) $\int \tan^3(x)\sec^2(x) dx$		10) $\int \cos(x)\sqrt{1 + \sin(x)} dx$	

Let  $u = (?)$ .

A. $u = \sin^3(x)$	D. $u = 1 + \sin(x)$	L. $u = \cos(x)$	M. $u = x^2$	O. $u = x^2 + 1$
P. $u = \sin(x)$	R. $u = \tan^3(x)$	S. $u = e^x$	(. $u = \tan(x)$	). $u = x^3 + 1$

L O O P  
8 1 1 6

D ( L O O P )  
10 9 7 2 3 5 4

## WHAT POLITICAL MOVEMENT AIMS TO PREVENT THE TEACHING OF CALCULUS IN HIGH SCHOOLS?

For the indefinite integrals 1) – 10) above, 1a) – 10a)  $du = (?)$ :

A. $du = 3x^2 dx$	B. $du = \tan(x) dx$	E. $du = 2x dx$	I. $du = -\sin(x) dx$
K. $du = \sec(x) dx$	M. $du = \sec^2(x) dx$	P. $du = \sin(x) dx$	R. $du = \tan^3(x) dx$
S. $du = e^x dx$	T. $du = \cos(x) dx$	U. $du = -\cos(x) dx$	V. $du = (x^3 + 1) dx$

For the indefinite integrals 1) – 10) above, 1b) – 10b) give the indefinite integral.

A. $\frac{1}{6}(x^2 + 1)^6 + k$	D. $\frac{1}{6}(x^3 + 1)^6 + k$	E. $\frac{2}{3}(x^2 + 1)^{3/2} + k$	H. $\frac{1}{4}\sin^4(x) + k$
M. $\frac{1}{4}\tan^4(x) + k$	N. $-\sec(x) + k$	O. $e^{\cos(x)} + k$	P. $\sec(x) + k$
P. $\sec^3(x) + k$	R. $\frac{2}{3}(\sin x + 1)^{3/2} + k$	T. $\ln(x^2 + 1) + k$	V. $\ln \sin(x)  + k$

T H E  
5a 5b 1a

A N T I -  
4a 8b 10a 7a

D E R I V A T I V E  
4b 3a 10b 8a 6b 1b 2b 8a 6b 1a

M O V E M E N T  
9a 7b 6b 2a 9b 3b 8b 6a

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$$u = x^2 + 1$$

$$\frac{du}{dx} = 2x$$

$$du = 2x dx$$

$$u = x^3 + 1$$

$$\frac{du}{dx} = 3x^2 dx$$

$$u = \sin x$$

$$du = \cos x dx$$

$$u = \cos x$$

$$du = -\sin x dx$$

$$u = \tan x$$

$$du = \sec^2 x dx$$

$$u = 1 + \sin x$$

$$du = \cos x dx$$

$$1) \int u^5 du$$

$$\frac{1}{6} u^6 + C$$

$$\frac{1}{6} (x^2 + 1)^6 + C$$

$$2) \int \frac{1}{u} du$$

$$\ln u + k$$

$$\ln |x^2 + 1| + k$$

$$3) \int \sqrt{u} du = \int u^{\frac{1}{2}} du$$

$$\frac{2}{3} u^{\frac{3}{2}} + k = \frac{2}{3} (x^2 + 1)^{\frac{3}{2}} + k$$

$$4) \int u^5 du$$

$$\frac{1}{6} u^6 + C$$

$$\frac{1}{6} (x^3 + 1)^6 + C$$

$$5) \int u^3 du$$

$$\frac{1}{4} u^4 + C$$

$$\frac{1}{4} (\sin^4 x) + C$$

$$6) \int \frac{1}{u} du$$

$$\ln u + C$$

$$\ln |\sin x| + C$$

$$7) \int e^u du$$

$$e^u + C$$

$$e^{\cos x} + C$$

$$8) \int \frac{1}{u^2} du$$

$$-u^{-1} + C$$

$$-\cos^{-1} x + C$$

$$-\frac{1}{\cos x} + C$$

$$-\sec x + C$$

$$9) \int u^3 du$$

$$\frac{1}{4} u^4 + C$$

$$\frac{1}{4} \tan^4 x + C$$

$$10) \int \sqrt{u} du$$

$$\frac{2}{3} u^{\frac{3}{2}} + k$$

$$\frac{2}{3} (1 + \sin x)^{\frac{3}{2}} + C$$