

Quadratic Equations

1. Standard Form: _____

The y-intercept is always (0, _____). The axis of symmetry is x = _____

Make up a quadratic equation in standard form and find the y-intercept and the axis of symmetry.

2. Vertex Form: _____

The vertex is always (_____, _____)

Make up a quadratic equation in vertex form and find the vertex.

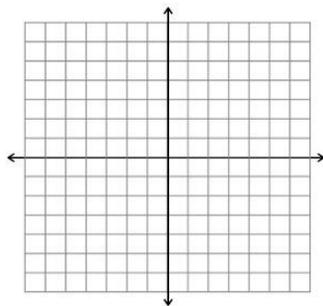
3. Intercept Form: _____

The x-intercepts are always (_____, 0) and (_____, 0)

Make up a quadratic equation in intercept form and find the x-intercepts.

4. Parent Function $y = x^2$

Graph:



Characteristic Points:

5. Transformations: $y = a(x \pm h)^2 \pm k$

What does ***h*** do? _____

What does ***k*** do? _____

What does ***a*** do? _____

What if ***a*** was negative? _____

Make up your own quadratic equation:

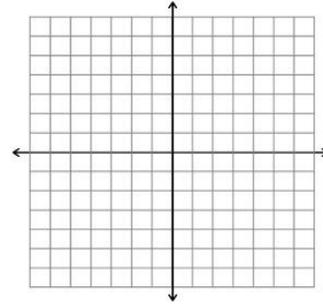
Describe the transformations:

What inequality symbols are used for the following?

Dashed parabola: _____

Shade up: _____

Graph it:



Solid parabola: _____

Shade down: _____

Graph each inequality.

$$y > -x^2 + 2x + 1$$

Standard form

vertex:

Find AOS first.

Plug AOS into equation to find y value of vertex.

Plot characteristic points up or down?

Solid or dotted?

Shade up or down?

$$y \leq 2(x-2)^2 - 3$$

vertex form

vertex:

Plot points up or down?

Characteristic points?

Solid or dotted?

Shade up or down?

$$y \geq (x-3)(x+1)$$

intercept form

x-int:

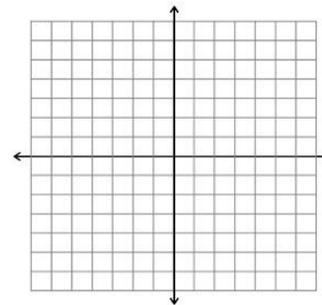
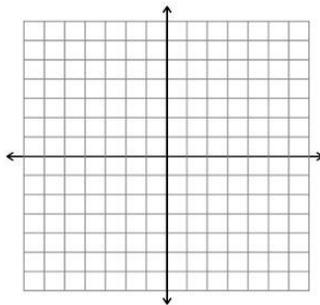
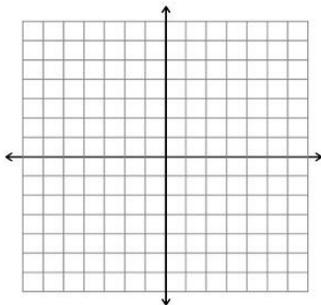
vertex:

AOS is in the middle between the x-intercepts.

Find y value of vertex.

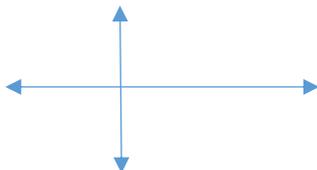
Plot Characteristic points up or down?

Solid or dotted? Shade up/down?



6. Solve by graphing:

Sketch what you see on your calculator



1. Get equation to equal _____

2. Enter the equation in _____ on the calculator.

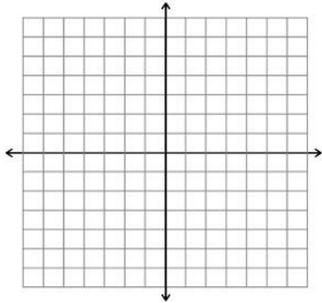
3. Have the calculator find the _____.

Practice: $x^2 = 10x - 21$ $x = \underline{\hspace{2cm}}$ or $x = \underline{\hspace{2cm}}$

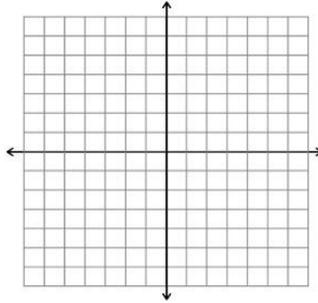
Remember a quadratic equation can have 2 real solutions, 1 real solutions or 2 imaginary solutions.

Sketch a graph that illustrates each.

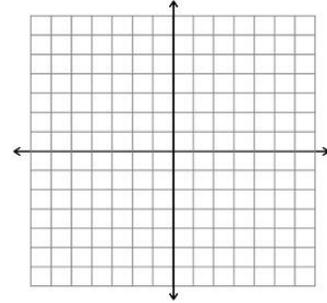
2 real solutions



1 real solution



imaginary solutions



- 7. Solve by factoring:**
1. Make sure the equation equals _____.
 2. Divide by the _____.
 3. If it is a trinomial that starts x^2 , find two numbers that _____ to get c, and _____ to get b.
 4. If it is a trinomial that starts ax^2 , rewrite as _____ terms and use grouping.
 5. If it is a binomial, check that is a difference square pattern, which is _____.

$$x^2 - 2x - 15 = 0$$

$$4y^2 - 25 = 0$$

$$2w^2 - 3w = 9$$

$$2a^2 + 60 = -22a$$

8. Solve by square roots: Use when there is only one x in the equation.

1. Isolate the radical.
2. _____ both sides to eliminate the exponent, creating two values, one _____ and one _____.
3. You will get an imaginary number when _____

$$3(x + 4)^2 - 18 = 0$$

$$4x^2 + 100 = 0$$

9. **Solve by completing the square:** Starting with $ax^2 + bx + c = 0$

1. Divide by a and move c to the other side.
2. Draw a square on each side.
3. Put _____ in each square.
4. Rewrite the left side as _____, and simplify the right side.
5. Square root both side. Don't forget the _____.

$$x^2 - 8x - 84 = 0$$

$$3x^2 + 6x - 12 = 0$$

10. **Solve using the quadratic formula.** Make sure the equation equals _____

The formula is $x =$ _____

$$6x^2 + x - 15 = 0$$

$$x^2 + 25 = 10x$$

11. Projectile Motion:

We want to know the **starting height** (which is _____ on the graph),
the **maximum height** and when it occurs (which is _____ on the graph),
and when the ball hits **the ground** (which is _____ on the graph).

- A rocket is fired into the air. Its height, in feet, is defined by the equation:
 $h(t) = -16t^2 + 64t + 2240$. Time is measured in seconds.

What is the starting height? _____

- A football is kicked into the air. Its height in meters after t seconds is given by $h(t) = -4.9(t - 2.4)^2 + 29$.

What is the maximum height of the ball? _____ When did it reach this height? _____

- An object is launched at 19.6 from a platform. The equation for the object's height s at time t seconds after launch is $h(t) = -4.9(t - 6)(t + 2)$, where s is in meters.

When did the object reach the ground? _____

12. Systems: Graph a system of equations using your calculator.

The solutions are the _____

Solve with a calculator: $\begin{cases} y = -2(x + 1)^2 + 1 \\ 2x + y = -3 \end{cases}$ _____

Graph the system: $\begin{cases} y \geq (x - 3)^2 - 6 \\ y > \frac{1}{2}x - 4 \end{cases}$

Parabola

Line

Vertex

y-intercept

Open up/down

slope

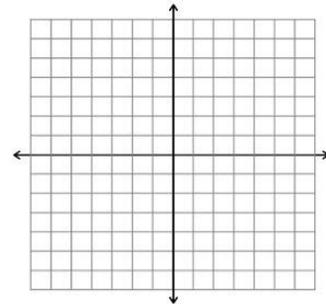
Characteristic pts.

Solid/dotted

Solid/dotted

Shade up/down

Shade up/down



Name a point that is part of the solution
