

p 215 #23

#26

1 a) 2 b) ∞

$$2a) y' = \frac{1 - y^4 - 2xy}{4xy^3 + x^2 - 3}$$

$$b) y' = \frac{y - 2x \cos y}{2 \cos 2y - x^2 \sin y - x}$$

} chp 3 review

$$*29 \quad c) y' = \frac{2x - y \cos(xy)}{x \cos(xy) + 1}$$

$$*36 \quad d) y' = \frac{\tan y}{1 - x \sec^2 y}$$

p 506 chp 7 review

#33

$$e) y' = (-2 \ln 2) x 2^{-x^2}$$

#35

$$f) \frac{x}{1+x^2} + \tan^{-1} x$$

#36

$$g) y' = \frac{2x}{(\ln 10)(1+x^2)}$$

#38

$$h) y' = y(\ln \cos x - x \tan x) \\ = (\cos x)^x (\ln \cos x - x \tan x)$$

#40

$$i) y' = \frac{1}{1 + (\sin^{-1} \sqrt{x})^2} \cdot \frac{1}{\sqrt{1-x}} \cdot \frac{1}{2\sqrt{x}}$$

#57

$$3a) y' = (2+x)(-e^{-x}) + e^{-x} \cdot 1 \\ y'(0) = -2 + 1 = -1 \\ y - 2 = -1(x - 0)$$

#58

$$b) y' = \ln x + 1 \\ y'(e) = 1 + 1 = 2 \\ y - e = 2(x - e)$$

p 215 #48

$$c) x^2 - 4xy + y^2 = 13 \\ 2x - (4y + 4xy') + 2yy' = 0 \\ 2 \cdot 2 - 4 \cdot 1 - 4(2)y' + 2(1)y' = 0 \\ -6y' = 0 \\ y' = 0$$

$$y - 1 = 0(x - 2)$$

$$y = 1$$

$$4) 2x + 2yy' = 0$$

$$2yy' = -2x$$

$$y' = \frac{-x}{y} \quad \text{at } (0,5) \quad y' = \frac{-0}{5} = 0$$

$$y'' = \frac{y(-1) - (-x)y'}{y^2}$$

$$y''(0,5) = \frac{5(-1) + (0)(0)}{5^2} = \frac{-5}{25} = -\frac{1}{5}$$

WHAT KIND OF FUNCTIONS DO GURUS AND THEIR DISCIPLES STUDY?

Find the derivative of each function and match with the result.

1) $y = e^{3x}$ $e^{3x} \cdot 3$ D	2) $y = \ln(2x)$ $\frac{1}{2x} \cdot 2$ N	3) $y = 2\sin(3x)$ $2[\cos(3x)] \cdot 3$ F	4) $y = \tan(x^2)$ $[\sec^2(x^2)] \cdot 2x$ J
5) $y = \frac{1}{2}\ln(x^2)$ $\frac{1}{2} \cdot \frac{1}{x^2} \cdot 2x$ N	6) $y = \ln(e^x)$ $\frac{1}{e^x} \cdot e^x = 1$ A	7) $y = x\cos(x)$ $1\cos x + x\sin x$ O	8) $y = xe^x$ $1e^x + xe^x$ K
9) $y = e^{\ln(x)}$ $e^{\ln x} \cdot \frac{1}{x} = 1$ A	10) $y = \sin(e^x)$ $[\cos(e^x)] \cdot e^x$ I	11) $y = \ln^2(x)$ $2\ln x \cdot \frac{1}{x}$ L	12) $y = e^{-\cos(x)}$ $e^{-\cos x} \cdot \sin x$ U
13) $y = \tan^2(x)$ $2[\tan x] \cdot \sec^2 x$ R	14) $y = -\frac{1}{x}\ln(x) = -x^{-1}\ln x$ $x^{-2}\ln x - x^{-1} \cdot \frac{1}{x}$ $\frac{\ln x}{x^2} - \frac{1}{x^2}$ T	15) $y = \ln(\cos(x))$ $\frac{1}{\cos x} \cdot -\sin x$ C	
16) $y = \frac{1}{x}\ln\left(\frac{1}{x}\right) = x^{-1}\ln(x^{-1})$ $-1x^{-2}\ln\left(\frac{1}{x}\right) + x^{-1} \cdot \frac{1}{x} \cdot -1x^{-2}$ $-\frac{1}{x^2}\ln\frac{1}{x} - \frac{1}{x^2} = \frac{1}{x^2}(-\ln x - 1)$ T		17) $y = xe^x + \ln(e^x) - x - 1$ $1e^x + xe^x + \frac{1}{e^x} \cdot e^x - 1 + 0$ E	

Derivatives.

A. $y' = 1$ G	B. $y' = x$	C. $y' = -\tan(x)$	D. $y' = 3e^{3x}$ J
E. $y' = xe^x + e^x$	F. $y' = 6\cos(3x)$	G. $y' = 6\sin(3x)$	H. $y' = \cos(3x)$
I. $y' = e^x\cos(e^x)$	L. $y' = \frac{2}{x}\ln(x)$	M. $y' = \frac{1}{x^2}$	N. $y' = \frac{1}{x}$
O. $y' = \cos(x) - x\sin(x)$	P. $y' = x\sin(x) - \cos(x)$	R. $y' = 2\tan(x)\sec^2(x)$	
S. $y' = 2x\sec^2(x^2)$	T. $y' = \frac{1}{x^2}(\ln(x) - 1)$	U. $y' = \sin(x)e^{-\cos(x)}$	

T R A N S C E N D E N T A L
14 13 6 2 4 15 17 5 1 8 5 16 9 11

F U N C T I O N S
3 12 5 15 14 10 7 2 4

WHICH LAW OF DIFFERENTIATION IS USED TO IMPRISON FUNCTIONS?

Derivatives of Composite Functions

If $y = f(g(x))$
then $y' = f'(g(x))g'(x)$

$y = 3\cos(2x^5)$
 $y' = -3\sin(2x^5) \cdot (10x^4)$
 $y' = -30x^4\sin(2x^5)$

Find the derivative y' of each function.

1) $y = (3x^2 + 1)^4$ $4(3x^2 + 1)^3 \cdot 6x$ E	2) $y = 3e^{2x^2}$ $3e^{2x^2} \cdot 4x$ E	3) $y = \sin(2x^3)$ $[\cos(2x^3)] \cdot 6x^2$ I	4) $y = 2\tan(x^5)$ $2[\sec^2(x^5)] \cdot 5x^4$ T
5) $y = \sqrt{3x^2 + 1}$ $\frac{1}{2}(3x^2 + 1)^{-\frac{1}{2}} \cdot 6x$ C	6) $y = \frac{-1}{3x^2 + 1}$ $-1(3x^2 + 1)^{-2} \cdot 6x$ A	7) $y = \ln(3x^2 + 1)$ $\frac{1}{3x^2 + 1} \cdot 6x$ L	8) $y = \cos\sqrt{x}$ $[-\sin x^{\frac{1}{2}}] \cdot \frac{1}{2}x^{-\frac{1}{2}}$ R
9) $y = e^{1/x}$ $e^{-x} \cdot -1x^{-2}$ N	10) $y = 3\sin^2(x)$ $6\sin x \cos x$ H	11) $y = \tan^5(2x)$ $5\tan^4(2x) \cdot \sec^2(2x) \cdot 2$ U	12) $y = 5 - 3\cos^2(x)$ $Y = -6\cos x \cdot -\sin x$ H

Derivatives.

A. $y' = \frac{6x}{(3x^2 + 1)^2}$	B. $y' = 6x\sqrt{3x^2 + 1}$	C. $y' = \frac{3x}{\sqrt{3x^2 + 1}}$	E. $y' = 24x(3x^2 + 1)^3$
E. $y' = 12xe^{2x^2}$	H. $y' = 6\sin(x)\cos(x)$	I. $y' = 6x^2\cos(2x^3)$	L. $y' = \frac{6x}{3x^2 + 1}$
M. $y' = \frac{1}{2\sqrt{x}} \cos\sqrt{x}$	N. $y' = -\frac{1}{x^2} e^{1/x}$	P. $y' = 2\sec^2(x^5)$	R. $y' = -\frac{1}{2\sqrt{x}} \sin\sqrt{x}$
S. $y' = 10\tan(2x)\sec(2x)$	T. $y' = 10x^4\sec^2(x^5)$	U. $y' = 10\sec^2(2x)\tan^4(2x)$	

T H E
4 10 1

C H A I N
5 12 6 3 9

R U L E
8 11 7 2